## Model Checking: From BDDs to Interpolation

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## Exercise 1

Write 2 CTL formulas.

1.  $f_1$  is true in a state iff the state is the start of a path along which p holds at least twice

2. f<sub>2</sub> is true in a state iff the state is the start of a path along which p holds exactly twice

## Exercise 2

- A Kripke structure M is represented by propositional formulas in CNF form as follows:
- •V=  $(v_1,...,v_n)$  is the vector of Boolean variables that represent the states
- $\cdot$ S(V) a CNF formula representing the set of states in M
- $\cdot R(V,V') a CNF$  formula representing the transition relation of M
- •AP = { $p_1$ ,..., $p_n$ } and for every  $p_i$  in AP,  $p_i(V)$  is a CNF formula representing the set of states in which  $p_i$  is true

## Exercise 2 (cont.)

Given two different states s, t, represented as CNF formulas.

Write a propositional formula  $f_k$ , which is satisfied iff there are two disjoined path of length k from s to t:

 $\pi$ = s,s<sub>1</sub>,...,s<sub>k</sub>,t and  $\pi$  = s',s'<sub>1</sub>,...,s'<sub>k</sub>,t' such that for every 1≤⁄i ≤k, L(s<sub>i</sub>) ⊆ L(s'<sub>i</sub>)